Zero-Shot Reinforcement Learning from Low Quality Data

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1 Motivation

- Behaviour Foundation Models (BFMs) based on forward-backward representations (FB) [1] and universal successor features (USF) [2] provide principled mechanisms for performing zero-shot task generalization.
- However, BFMs assume access to idealised (large & diverse) pre-training datasets that we can't expect for real problems.
- Can we pre-train BFMs on realistic (small & narrow) datasets?

2 Background

Forward-backward (FB) BFMs model the environment dynamics using *successor measures* which are the expected discounted time spent in subsets of future states:

 $M^{\pi}(s_0, a_0, S_+) := \sum_{t=0}^{T-1} \gamma^t \Pr(s_{t+1} \in S_+ | (s_0, a_0), \pi), \ \forall \ S_+ \subset \mathcal{S}.$

Together, a forward model F and backward model B approximate successor measures for all policies

 $M^{\pi_z}(s_0, a_0, X) \approx \int_X F(s_0, a_0, z)^\top B(s) \rho(\mathrm{d}s)$ $\forall \ s_0 \in \mathcal{S}, a_0 \in \mathcal{A}, X \subset \mathcal{S}, z \in \mathbb{R}^d,$ $\forall (s,a) \in \mathcal{S} \times \mathcal{A}, z \in \mathbb{R}^d$ $\pi(s, z) \approx \max_{a} F(s, a, z)^{\top} z$

Zero-shot RL:

Pre-train on reward-free dataset $\mathcal{D} = \{(s_i, a_i, s_{i+1})\}_{i=1}^{|\mathcal{D}|}$ Infer task from $\mathcal{D}_{\text{labelled}} = \{(s_i, R_{\text{eval}}(s_i))\}_{i=1}^{10,000}$

3 Failure Mode on Low Quality Datasets

The FB loss relies on actions sampled from the policy, and these may not exist in the dataset (*i.e.* they can be out-of-distribution (OOD)).

 $\mathcal{L}_{\text{FB}} = \mathbb{E}_{(s_t, a_t, s_{t+1}, s_{+}) \sim \mathcal{D}, z \sim \mathcal{Z}} [(F(s_t, a_t, z)^\top B(s_{+}) - \gamma \bar{F}(s_{t+1}, \underbrace{\pi_z(s_{t+1})}_{, z}, z)^\top \bar{B}(s_{+}))^2 - 2F(s_t, a_t, z)^\top B(s_{t+1})]$

This leads to value function overestimation at OOD state-action pairs:



Figure 1: **FB value overestimation with respect to dataset size and quality**. Log Q values and IQM of rollout performance on all Maze tasks for RND and Random datasets.

Conservative Behaviour Foundation Models





Figure 2: Conservative BFMs. (Left) Zero-shot RL methods must generalize to any task in z-space. (Middle) FB overestimates the value of actions not in the dataset. (*Right*) VC-FB suppresses the value of actions not in the dataset.

Value-Conservative Forward Backward Representations

 $\mathcal{L}_{\text{VC-FB}} = \alpha \cdot (\mathbb{E}_{s \sim \mathcal{D}, a \sim \mu(a|s), z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, a, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, z, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, z, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, z, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, z, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}} [F(s, z, z)^{\top} z] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal$

Measure-Conservative Forward Backward Representations

 $\mathcal{L}_{\text{MC-FB}} = \alpha \cdot (\mathbb{E}_{s \sim \mathcal{D}, a \sim \mu(a|s), z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{Z}, s_+ \sim \mathcal{D}}[F(s, a, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{D}, z \sim \mathcal{D}}[F(s, z, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{D}}[F(s, z, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal{D}, z \sim \mathcal{D}}[F(s, z, z)^\top B(s_+)] - \mathbb{E}_{(s, a) \sim \mathcal$

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Figure 3: Didactic example. The agents are tasked with learning separate policies for reaching (*) and (*). (a) RND dataset with all "left" actions removed (b) Best FB rollout after 1 million steps. (c) Best VC-FB performance after 1 million learning steps.

5 Setup

Baselines

- Zero-shot RL: FB, SF-LAP [5]
- Goal-conditioned RL: GC-IQL [6]
- Offline RL: CQL [7]

Environments

• ExORL & D4RL

Datasets

Random-100k









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$$\mathcal{H}(\mu)) + \mathcal{L}_{\mathrm{FE}}$$

$$[s_+)] - \mathcal{H}(\mu)) + \mathcal{L}_{ ext{FB}}$$











Figure 4: Aggregate ExORL Performance. Both conservative BFM variants stochastically dominate vanilla FB.



Figure 6: ExORL Performance by dataset/domain.

Limitations

- Absolute ExORL performance remains poor compared to methods trained on large/diverse datasets.
- Performance is sensitive the choice of τ which selects the degree of conservatism. IQL-style regularization would likely mitigate this. (*c.f.* D4RL performance)

References

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[4] Aviral Kumar, Justin Fu, Matthew Soh, George Tucker, and Sergey Levine. *Stabilizing off-policy*

q-learning via bootstrapping error reduction. NeurIPS 2019

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Figure 5: D4RL Performance. Conservative BFMs outperform vanilla BFMs, but do not match the performance of the single-task baseline.



variants increases as dataset size decreases.







